

4.3

Exercise Set

FOR EXTRA HELP



Concept Reinforcement In each of Exercises 1–10, match the set with the most appropriate choice from the column on the right.

- (h)** $\{x \mid x < -2 \text{ or } x > 2\}$
- (j)** $\{x \mid x < -2 \text{ and } x > 2\}$
- (f)** $\{x \mid x > -2\} \cap \{x \mid x < 2\}$
- (a)** $\{x \mid x \leq -2\} \cup \{x \mid x \geq 2\}$
- (e)** $\{x \mid x \leq -2\} \cup \{x \mid x \leq 2\}$
- (d)** $\{x \mid x \leq -2\} \cap \{x \mid x \leq 2\}$
- (b)** $\{x \mid x \geq -2\} \cap \{x \mid x \geq 2\}$
- (g)** $\{x \mid x \geq -2\} \cup \{x \mid x \geq 2\}$
- (c)** $\{x \mid x \leq 2\} \text{ and } \{x \mid x \geq -2\}$
- (i)** $\{x \mid x \leq 2\} \text{ or } \{x \mid x \geq -2\}$

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- \mathbb{R}
- \emptyset

Find each indicated intersection or union.

- $\{5, 9, 11\} \cap \{9, 11, 18\}$ $\{9, 11\}$
- $\{2, 4, 8\} \cup \{8, 9, 10\}$ $\{2, 4, 8, 9, 10\}$
- $\{0, 5, 10, 15\} \cup \{5, 15, 20\}$ $\{0, 5, 10, 15, 20\}$
- $\{2, 5, 9, 13\} \cap \{5, 8, 10\}$ $\{5\}$
- $\{a, b, c, d, e, f\} \cap \{b, d, f\}$ $\{b, d, f\}$
- $\{a, b, c\} \cup \{a, c\}$ $\{a, b, c\}$
- $\{r, s, t\} \cup \{r, u, t, s, v\}$ $\{r, s, t, u, v\}$
- $\{m, n, o, p\} \cap \{m, o, p\}$ $\{m, o, p\}$
- $\{3, 6, 9, 12\} \cap \{5, 10, 15\}$ \emptyset
- $\{1, 5, 9\} \cup \{4, 6, 8\}$ $\{1, 4, 5, 6, 8, 9\}$
- $\{3, 5, 7\} \cup \emptyset$ $\{3, 5, 7\}$
- $\{3, 5, 7\} \cap \emptyset$ \emptyset

Graph and write interval notation for each compound inequality.

- $3 < x < 7$
- $0 \leq y \leq 4$
- $-6 \leq y \leq 0$
- $-9 \leq x < -5$
- $x < -1 \text{ or } x > 4$
- $x < -5 \text{ or } x > 1$
- $x \leq -2 \text{ or } x > 1$
- $x \leq -5 \text{ or } x > 2$
- $x > -2 \text{ and } x < 4$
- $x > -7 \text{ and } x < -2$

- $-4 \leq -x < 2$
- $3 > -x \geq -1$
- $5 > a \text{ or } a > 7$
- $t \geq 2 \text{ or } -3 > t$
- $x \geq 5 \text{ or } -x \geq 4$
- $-x < 3 \text{ or } x < -6$
- $7 > y \text{ and } y \geq -3$
- $6 > -x \geq 0$
- $x < 7 \text{ and } x \geq 3$
- $x \geq -3 \text{ and } x < 3$
- Aha!** $t < 2 \text{ or } t < 5$
- $t > 4 \text{ or } t > -1$

Solve and graph each solution set.

- $-2 < t + 1 < 8$
- $-3 < t + 1 \leq 5$
- $4 < x + 4 \text{ and } x - 1 < 3$
- $-1 < x + 2 \text{ and } x - 4 < 3$
- $-7 \geq 2a - 3 \text{ or } 3a + 1 > 7$
- $-4 \leq 3n + 5 \text{ or } 2n - 3 \leq 7$
- Aha!** $x + 7 \leq -2 \text{ or } x + 7 \geq -3$
- $x + 5 < -3 \text{ or } x + 5 \geq 4$
- $-7 \leq 4x + 5 \leq 13$
- $-4 \leq 2x + 3 \leq 15$
- $5 > \frac{x-3}{4} > 1$
- $3 \geq \frac{x-1}{2} \geq -4$

57. $-2 \leq \frac{x+2}{-5} \leq 6$ □

58. $-10 \leq \frac{x+6}{-3} \leq -8$ □

59. $2 \leq f(x) \leq 8$, where $f(x) = 3x - 1$ □

60. $7 \geq g(x) \geq -2$, where $g(x) = 3x - 5$ □

61. $-21 \leq f(x) < 0$, where $f(x) = -2x - 7$ □

62. $4 > g(t) \geq 2$, where $g(t) = -3t - 8$ □

63. $f(t) < 3$ or $f(t) > 8$, where $f(t) = 5t + 3$ □

64. $g(x) \leq -2$ or $g(x) \geq 10$, where $g(x) = 3x - 5$ □

65. $6 > 2a - 1$ or $-4 \leq -3a + 2$ □

66. $3a - 7 > -10$ or $5a + 2 \leq 22$ □

67. $a + 3 < -2$ and $3a - 4 < 8$ □

68. $1 - a < -2$ and $2a + 1 > 9$ □

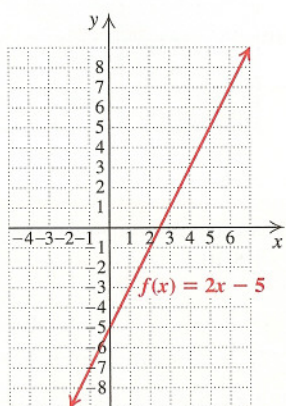
69. $3x + 2 < 2$ and $3 - x < 1$ ∅

70. $2x - 1 > 5$ and $2 - 3x > 11$ ∅

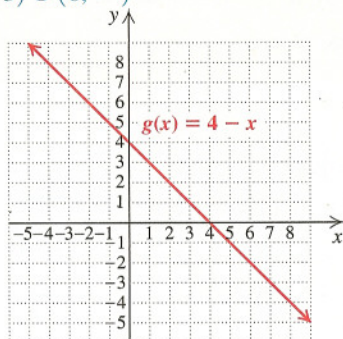
71. $2t - 7 \leq 5$ or $5 - 2t > 3$ □

72. $5 - 3a \leq 8$ or $2a + 1 > 7$ □

73. Use the accompanying graph of $f(x) = 2x - 5$ to solve $-7 < 2x - 5 < 7$. $(-1, 6)$



74. Use the accompanying graph of $g(x) = 4 - x$ to solve $4 - x < -2$ or $4 - x > 7$. $(-\infty, -3) \cup (6, \infty)$



For $f(x)$ as given, use interval notation to write the domain of f .

75. $f(x) = \frac{9}{x+8}$
 $(-\infty, -8) \cup (-8, \infty)$

76. $f(x) = \frac{2}{x+3}$
 $(-\infty, -3) \cup (-3, \infty)$

77. $f(x) = \frac{-8}{x}$
 $(-\infty, 0) \cup (0, \infty)$

78. $f(x) = \frac{x+3}{2x-8}$
 $(-\infty, 4) \cup (4, \infty)$

79. $f(x) = \sqrt{x-6}$ $[6, \infty)$

80. $f(x) = \sqrt{x-2}$

81. $f(x) = \sqrt{2x+7}$ $[-\frac{7}{2}, \infty)$

82. $f(x) = \sqrt{8-5x}$ $(-\infty, \frac{8}{5}]$

83. $f(x) = \sqrt{8-2x}$ $(-\infty, 4]$

84. $f(x) = \sqrt{10-2x}$ $(-\infty, 5]$

Use interval notation to write each domain.

85. The domain of $f + g$, if $f(x) = \sqrt{x-5}$ and $g(x) = \sqrt{\frac{1}{2}x+1}$ $[5, \infty)$

86. The domain of $f - g$, if $f(x) = \sqrt{x+3}$ and $g(x) = \sqrt{2x-1}$ $[\frac{1}{2}, \infty)$

87. The domain of $f \cdot g$, if $f(x) = \sqrt{3-x}$ and $g(x) = \sqrt{3x-2}$ $[\frac{2}{3}, 3]$

88. The domain of $f + g$, if $f(x) = \sqrt{3-4x}$ and $g(x) = \sqrt{x+2}$ $[-2, \frac{3}{4}]$

TW 89. Why can the conjunction $2 < x$ and $x < 5$ be rewritten as $2 < x < 5$, but the disjunction $2 < x$ or $x < 5$ cannot be rewritten as $2 < x < 5$?

TW 90. Can the solution set of a disjunction be empty? Why or why not?

SKILL REVIEW

To prepare for Section 4.4, review absolute value and graphing (Sections 1.2 and 2.2).

Find the absolute value. [1.2]

91. $|-5 - 2|$ 7

92. $|6 - 0|$ 6

Graph. [2.2]

93. $g(x) = 2x$ □

94. $f(x) = 4$ □

95. $g(x) = -3$ □

96. $f(x) = |x|$ □

SYNTHESIS

TW 97. What can you conclude about a , b , c , and d , if $[a, b] \cup [c, d] = [a, d]$? Why?

TW 98. What can you conclude about a , b , c , and d , if $[a, b] \cap [c, d] = [a, b]$? Why?

99. **Counseling.** The function given by $s(t) = 500t + 16,500$ can be used to estimate the number of student visits to Cornell University's counseling center t years after 2000. For what years is the number of student visits between 18,000 and 21,000? **Between 2003 and 2009**

Source: Based on data from Cornell University

- 100. Pressure at Sea Depth.** The function given by $P(d) = 1 + (d/33)$ gives the pressure, in atmospheres (atm), at a depth of d feet in the sea. For what depths d is the pressure at least 1 atm and at most 7 atm? $0 \text{ ft} \leq d \leq 198 \text{ ft}$
- 101. Converting Dress Sizes.** The function given by $f(x) = 2(x + 10)$ can be used to convert dress sizes x in the United States to dress sizes $f(x)$ in Italy. For what dress sizes in the United States will dress sizes in Italy be between 32 and 46?
 Sizes between 6 and 13
- 102. Solid-Waste Generation.** The function given by $w(t) = 0.0125t + 4.525$ can be used to estimate the number of pounds of solid waste, $w(t)$, produced daily, on average, by each person in the United States, t years after 2000. For what years will waste production range from 4.6 lb to 4.8 lb per person per day? *From 2006 through 2022*
- 103. Body-Fat Percentage.** The function given by $F(d) = (4.95/d - 4.50) \times 100$ can be used to estimate the body fat percentage $F(d)$ of a person with an average body density d , in kilograms per liter. A woman's body fat percentage is considered acceptable if $25 \leq F(d) \leq 31$. What body densities are considered acceptable for a woman?
 Densities between 1.03 kg/L and 1.04 kg/L
- 104. Minimizing Tolls.** A \$6.00 toll is charged to cross the bridge from mainland Florida to Sanibel Island. A six-month reduced-fare pass, costing \$50.00, reduces the toll to \$2.00. A six-month unlimited-trip pass costs \$300 and allows free crossings. How many crossings in six months does it take for the reduced-fare pass to be the more economical choice?
 Source: www.leewayinfo.com
 More than 12 trips and fewer than 125 trips



Solve and graph.

- 105.** $4m - 8 > 6m + 5$ or $5m - 8 < -2$
- 106.** $4a - 2 \leq a + 1 \leq 3a + 4$
- 107.** $3x < 4 - 5x < 5 + 3x$
- 108.** $x - 10 < 5x + 6 \leq x + 10$

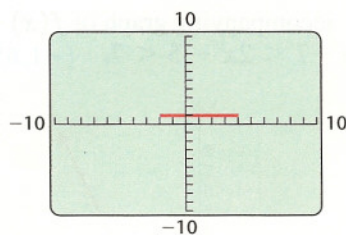
Determine whether each sentence is true or false for all real numbers a , b , and c .

- 109.** If $-b < -a$, then $a < b$. *True*
- 110.** If $a \leq c$ and $c \leq b$, then $b > a$. *False*
- 111.** If $a < c$ and $b < c$, then $a < b$. *False*
- 112.** If $-a < c$ and $-c > b$, then $a > b$. *True*

For $f(x)$ as given, use interval notation to write the domain of f .

- 113.** $f(x) = \frac{\sqrt{3 - 4x}}{x + 7}$ $(-\infty, -7) \cup (-7, \frac{3}{4}]$
- 114.** $f(x) = \frac{\sqrt{5 + 2x}}{x - 1}$ $[-\frac{5}{2}, 1) \cup (1, \infty)$

- 115.** On many graphing calculators, the TEST key provides access to inequality symbols, while the LOGIC option of that same key accesses the conjunction *and* and the disjunction *or*. Thus, if $y_1 = x > -2$ and $y_2 = x < 4$, Exercise 31 can be checked by forming the expression $y_3 = y_1 \text{ and } y_2$. The interval(s) in the solution set appears as a horizontal line 1 unit above the x -axis. (Be careful to “deselect” y_1 and y_2 so that only y_3 is drawn.) Use the TEST key to check Exercises 35, 39, 41, and 43.



Try Exercise Answers: Section 4.3

- 11.** $\{9, 11\}$ **13.** $\{0, 5, 10, 15, 20\}$
- 27.** $\leftarrow \begin{array}{c} | \\ -10 \end{array} \begin{array}{c} | \\ 4 \end{array} \rightarrow (-\infty, -1) \cup (4, \infty)$
- 31.** $\leftarrow \begin{array}{c} | \\ -2 \end{array} \begin{array}{c} | \\ 4 \end{array} \rightarrow (-2, 4)$
- 45.** $\{t | -3 < t < 7\}$, or $(-3, 7)$ $\leftarrow \begin{array}{c} | \\ -3 \end{array} \begin{array}{c} | \\ 7 \end{array} \rightarrow$
- 49.** $\{a | a \leq -2 \text{ or } a > 2\}$, or $(-\infty, -2] \cup (2, \infty)$
- $\leftarrow \begin{array}{c} | \\ -2 \end{array} \begin{array}{c} | \\ 2 \end{array} \rightarrow$ **51.** \mathbb{R} , or $(-\infty, \infty)$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \rightarrow$
- 65.** $\{a | a < \frac{7}{2}\}$, or $(-\infty, \frac{7}{2})$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ \frac{7}{2} \end{array} \rightarrow$
- 67.** $\{a | a < -5\}$, or $(-\infty, -5)$ $\leftarrow \begin{array}{c} | \\ -5 \end{array} \begin{array}{c} | \\ 0 \end{array} \rightarrow$ **69.** \emptyset
- 79.** $[6, \infty)$ **85.** $[5, \infty)$

- 105.** $\{m | m < \frac{6}{5}\}$, or $(-\infty, \frac{6}{5})$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ \frac{6}{5} \end{array} \rightarrow$
- 106.** $\{a | -\frac{3}{2} \leq a \leq 1\}$, or $[-\frac{3}{2}, 1]$; $\leftarrow \begin{array}{c} | \\ -\frac{3}{2} \end{array} \begin{array}{c} | \\ 1 \end{array} \rightarrow$
- 107.** $\{x | -\frac{1}{8} < x < \frac{1}{2}\}$, or $(-\frac{1}{8}, \frac{1}{2})$ $\leftarrow \begin{array}{c} | \\ -\frac{1}{8} \end{array} \begin{array}{c} | \\ \frac{1}{2} \end{array} \rightarrow$
- 108.** $\{x | -4 < x \leq 1\}$, or $(-4, 1]$; $\leftarrow \begin{array}{c} | \\ -4 \end{array} \begin{array}{c} | \\ 1 \end{array} \rightarrow$